

On the Relationship between the Underwater Acoustic and Optical Channels

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Abstract

Wireless transmissions in water are mostly carried out via long-range (but low-rate) underwater acoustic communications, or short-range (but high-rate) underwater optical communications. In this paper we are interested in finding whether a statistical relationship exists between underwater acoustics and optics. Besides the theoretical interest of such relationship, predicting the quality of the optical link through acoustics is also relevant in the context of a multimodal system with both acoustics and optics. Our study is based on a large dataset acquired during the NATO ALOMEX'2015 expedition. During this experiment, we simultaneously measured several characteristics of the acoustic and optical links at multiple locations, reflecting a diversity of sea environments. Our results, show a strong correlation between the properties of the acoustic link and the reliability of optical communications. This correlation makes it possible to predict the state of the underwater optical link at a certain depth and range. Due to the complexity of the acoustic and optical channels, we could not find the source of this correlation. This work is therefore aimed to stimulate a theoretical study of the mutual properties of underwater acoustic and optical communication links. For reproducibility, we share the processed data from the experiment.

Index Terms

Underwater acoustic communications; Underwater optical communications; Multimodal systems; Support vector machine; Machine learning; Classification; Prediction; Sea Experiment

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I. INTRODUCTION

In the last decade, ocean exploration has increased considerably through underwater surveys. The purposes of these surveys include bathymetry mapping and natural resource prospection, maintenance (environmental monitoring and structural inspection of underwater facilities such as drilling devices and pipelines), and securing marine infrastructures against intruders. The ability to wirelessly exchange information among submerged devices is a key enabling technology to perform these tasks. Currently, the two top technologies for underwater wireless transmission are underwater acoustic communications (AC) and underwater optical communications (OC). AC is characterized by long-range (in the order of tens of km) but low-data-rate transmissions (up to a few kbps), and is considered highly unreliable due to the limited bandwidth, long delay spread, short channel coherence time, and dispersiveness that characterize the acoustic channel [1]. OC features high data rates (in the order of Mbps), but is only suitable over much shorter transmission ranges (in the order of tens of meters) [2].

AC and OC are driven by different physics. The former involves the propagation of a pressure wave and is modeled, e.g., via the so-called normal modes [3], [4] or empirical equations [5], whereas the latter is performed via electromagnetic waves whose propagation is driven by the radiative transfer equations [6]. The sources of noise in the underwater acoustic channel are also much different than those that affect the optical channel [7]. While shipping noise and sea waves are the main sources of noise in AC [3], the irradiance and scattering of sunlight in the water are the main factors that affect OC. Although these models are seemingly unrelated, it is of theoretical interest to show if there exists a combination of underwater acoustic properties that can be exploited to predict the state of the underwater optical link. Specifically, we are mainly interested in finding a relationship between the measured physical characteristics of the underwater acoustic link and the following two estimates:

- 1) a binary (good/bad) state of OC at a certain range and depth;
- 2) the signal-to-noise ratio (SNR) of OC at a given range and depth.

The first item is a classification problem, whereas the second item implies a regression and

prediction problem.

While finding a relation between the AC and OC is of theoretical interest per se, such relation also has several practical applications. First, it would assist in predicting the characteristics of OC through AC. This will significantly reduce the cost and complexity of obtaining OC measurements, which otherwise require specialized equipment [8], [9]. Second, by predicting the quality of OC through AC, a mobile node which holds both communication systems can be guided to a location where both technologies can be efficiently used. This application is specifically important for multimodal underwater communication systems, where both OC and AC are utilized [10]. For example, by predicting the properties of OC, an autonomous underwater vehicle (AUV) equipped with both AC and OC [11] can be directed to the maximal¹ range and depth still allowing reliable communication with the hub. Third, exploiting a relationship between OC and AC would enable more effective switching mechanisms than the current range-based triggering of OC, which only reflects the communication system specifications, and not the actual characteristics of the communication channel [7].

In this work, we study the relationship between AC and OC from a statistical point of view. Specifically, we investigate whether, for a given range and depth, the properties of an underwater AC link can be used for classifying OC link quality and for predicting the SNR over OC links. We limit our application to environments like the open sea, where it can be assumed that the properties of the optical link change slowly in time and space. While we were unable to find a theoretical/mathematical explanation for the relation between the AC and the OC, we present statistical evidence that this relation exists. It is our hope to stimulate further theoretical investigations in this direction.

Our study is based on a large dataset of acoustic and optical link properties simultaneously measured over a prolonged time span and over different frequency bands. Our dataset was obtained during the ALOMEX 2015 experiment led by the NATO STO CMRE, La Spezia, Italy. Using this

¹For safety reasons, the AUV should avoid a close contact with the receiver.

dataset, we trained different learning models based on support vector machines (SVMs) [12], with the goal of classifying the corresponding quality of the optical link and predicting the optical SNR at various distances and depths. The learning system was designed and tuned to maximize the classification and prediction accuracy, while at the same time avoiding overfitting.

Our results show a strong correlation between the properties of the underwater acoustic link and the overall quality of OC. Moreover, using the acoustic properties as predictors, we show that the SNR of the OC link can be estimated with a sufficient degree of accuracy to enable ambient intelligence in underwater communication systems. This surprising result not only provides a tool for combining AC and OC, but also justifies further theoretical studies targeting the relationship between the underwater acoustic and optical links. Our contribution is therefore three-fold and includes:

- 1) an extensive quantitative study of the relationship between AC and OC;
- 2) a comparison between such relation at different acoustic frequency bands;
- 3) a dataset freely shared with the community for further investigation of the link between underwater acoustics and optics, and for the design of multimodal AC/OC systems.

The remainder of this paper is organized as follows. An overview of AC, OC, and multimodal systems is given in Section II, which also provides the basics of the machine learning techniques employed for data analysis. A detailed description of the acquired dataset is given in Section III. The methods and results of the quantitative study are described in Section IV. Finally, we draw our conclusions in Section V.

II. PRELIMINARIES

A. Basics of AC

Substantial differences exist between long-range deep water AC and short-range shallow water AC. Since multimodal systems are used for relatively short ranges of a few km, we focus on the latter. The shallow water underwater channel is a time-varying frequency-selective channel, characterized by a long delay spread [13] and a coherence time on the order of tens of ms [14].

Given the low transmission rate (common systems achieve a few kbps [15]), such long channel and short coherence time pose a challenge for channel equalization [16]. Since the sea surface is continuously in motion, individual channel taps are affected by a Doppler shift that, depending on the carrier frequency, may vary up to tens of Hz [17]. Due to the low sound speed (roughly 1500 m/s), this Doppler shift affects the duration of the received signal and, therefore, cannot be fully compensated by a phase-locked loop. Instead, interpolation is generally required [18]. The key parameters to predict the integrity of AC are the number of channel taps, their power and propagation delay, and the variation of these characteristics over time.

Besides the channel impulse response and the power attenuation, AC is also highly affected by the channel ambient noise. The ambient noise is usually modeled as an isotropic colored Gaussian noise whose power spectral density reduces by 10 dB per octave [19]. However, the acoustic ambient noise may also include location-dependent, non-isotropic noise which may affect the performance of AC. The sources of such noise are acoustic transmissions from nearby ships, short noise transients from marine fauna such as snapping shrimps, and wideband noise from breaking waves, especially when the receiver is close to the water surface [20]. Thus, besides the noise level itself, the time-varying characteristics of the noise also affect the performance of AC.

The SNR (in dB) of a transmission performed at a frequency f_a over a distance d between the transmitter and the receiver is found as [3]

$$SNR(d, f_a) = 10 \log_{10} \left(\frac{P_a}{N(f_a) \delta f_a} \right) - A(d, f_a), \quad (1)$$

where P_a is the source level (usually expressed in dB relative to 1 μ Pa @ 1 m from the source), $N(f_a)$ is the noise level, $A(d, f_a)$ is the power attenuation in dB, and δf_a is a narrow band around f_a where we can assume $A(d, f) = A(d, f_a)$ and $N(f) = N(f_a)$.

B. Basics of OC

Light traveling in the water interacts with the particulates and dissolved materials within the water as well as the water molecules themselves. These interactions produce light attenuation (modeled via an attenuation rate per unit length traveled by the wave, and termed c) that will

determine the underwater light field, or radiance, denoted as L , and defined as the measure of light energy leaving an extended source in a particular direction.

The parameters L and c are related through the radiative transfer equation (RTE), which relates the apparent and inherent optical properties of the medium [6]. The light attenuation rate c , the optical absorption rate a , and the loss rate due to scattering processes b are related as

$$c = a + b . \quad (2)$$

If the inherent optical properties of the medium depend only on depth, inelastic processes are ignored, and there are no internal sources, the time-dependent RTE is described as [21]

$$\cos \theta \frac{dL(z, \lambda, \theta, \phi)}{dz} = -c(z, \lambda)L(z, \lambda, \theta, \phi) + \int_{4\pi} \beta(z, \lambda, \theta', \phi' \rightarrow \theta, \phi) L(z, \lambda, \theta', \phi') d\Omega' , \quad (3)$$

where $\beta(\cdot)$ is called the volume scattering function and describes how the medium scatters light per unit length and solid angle. The polar angle θ and the azimuthal angle ϕ of a spherical coordinate system specify the scattered light direction, whereas the coordinates (θ', ϕ') inside the integral convey the direction of the incident light. The integration limit denotes that the integral is computed over the unit sphere surface, and we recall that $d\Omega' = \sin \theta' d\theta' d\phi'$. At a given depth and wavelength, L is usually referred to as the radiance distribution. The first term on the right hand side of (3) represents the loss of radiance in the direction (θ, ϕ) due to scattering and absorption, while the second term provides the gain in radiance from all other directions (θ', ϕ') into the direction (θ, ϕ) . Analytical solutions of the RTE (3) are possible only if scattering is negligible. Otherwise, as in the present work, (3) must be solved numerically. The most complete and accurate method to do so is the successive-orders-of-scattering solution used in radiative transfer modeling software such as Hydrolight [21].

Because radiance is difficult to measure, most light field measurements involve integrals of the radiance distribution. For this study, we are interested in scalar irradiance, E_0 , i.e., the irradiance measured over all directions, obtained by integrating radiance over the whole sphere as

$$E_0(z, \lambda) = \int_{4\pi} L(z, \lambda, \theta, \phi) d\Omega . \quad (4)$$

In the case of light transmission for underwater optical communications, this will be affected by the ambient light, considered as noise. The ambient light noise power N_A is obtained as

$$N_A = (S \cdot E_0 \cdot A_r)^2, \quad (5)$$

where S is the sensitivity of the receiver and A_r is the receiver area.

In this work, we aim to prove a connection between the underwater acoustic channel and the optical channel to predict the SNR of an optical communication system. While the literature includes optical communication systems with range of hundreds of meters [22], these works use a highly-directive laser source that requires perfect alignment between the transmitter and the receiver, and assume very clear water ($c = 0.063$ 1/m). Instead, we consider a LED-based optical communication system whose semiaperture angle is three orders of magnitude larger than the lasers, and thus imposes fewer limitations on system alignment. The considered system includes a LED transmitter [23], and a Si PIN Hamamatsu photodiode [2] receiver. The achievable range is between 2 and 50 m, depending on the water turbidity and the surrounding light noise. However, we note that in this work we measured general underwater optical channel parameters. Thus, we do not limit our conclusions to a certain type of optical system, and our conclusions regarding the observed correlation between the underwater acoustic channel and the optical channel also apply to e.g., laser-based underwater optical systems.

C. Intuitive Explanation for a Correlation between AC and OC

This paper focuses on presenting evidence about a correlation between AC and OC that allows the classification of OC and the prediction of its SNR based on AC data. In the absence of a well established theory for the relation between the two channels, in this section we give our intuitive explanation for this correlation. Our main claim is that the quality of OC is mostly affected by the turbidity of the water, and that this turbidity is generated by channel parameters that also affect AC.

We start with the connection between acoustic noise and OC. The acoustic noise at shallow water is dominated by the acoustic noise generated by the surface waves. Close to the surface,

these waves generate water bubbles and are a main contributor to the optical turbidity. Hence, the noise level and the acoustical SNR are expected to have some relation with OC. Similarly, the quality (or integrity) of AC that is affected by the acoustic noise is expected to have some link to OC as well.

The optical turbidity is also very much affected by the number of scatterers in the water column, for example plankton and floating sediments. These scatterers often also serve as acoustic volume reflectors, which affect the structure of the underwater acoustic impulse response. Hence, we expect that parameters like the channel's length, the delay spread, and the number of taps, will have some connection with the optical turbidity and therefore with the quality of OC. We also see a relation between the number of scatterers in the water, which affects both the AC and the OC. Specifically, the volume scatterers affect the optical propagation in water as well as the RMS of the AC's channel taps. Moreover, the number of scatterers in the channel is proportional to the acoustic power absorption, and thus affects the received signal level of the AC.

Last, we note that the time dependency of AC is mostly affected by the motion in the channel. In turn, this motion creates circulation in the water, that highly affects the water's turbidity. Hence, we expect to find a connection between the OC and measures like the channel coherence time and the noise level coherence time that reflect the time-dependency of the channel.

D. Overview of Multimodal Systems

Multimodal systems combine AC with optical [2], [11] or radiofrequency [24], [25] communications, as well as AC systems working in different bands [26], [27]. Among these, OC seems to be the most mature alternative to AC. In [28], a proof-of-concept for Orthogonal frequency-division multiplexing (OFDM) based OC is described, and in [11] the capabilities of OC are demonstrated for transmission of video over ranges of a few meters. Multimodal systems combining AC and OC mostly involve a separate control over these two technologies. In [29], the sink-to-node downlink is based on AC, and the uplink is serviced through OC. A similar concept is suggested in [30], [31] where AC is used to request AUVs to approach and collect data through OC. On the contrary,

in [32], OC is employed for positioning of a swarm of AUVs, and AC is used for data exchange between the AUVs.

A few works suggested a mechanism to switch between AC and OC so that data exchange could be efficiently managed based on the current communication capabilities. This includes a switching strategy based on the received power for each link [7], or based on the estimated distance between the transmitter and the receiver [33]. MURAO is the first multimodal opto-acoustic routing protocol [34]. It uses acoustic communications to help manage routing in a clustered multihop optical network. The longer range acoustics connects cluster heads, thereby allowing sharing of cluster information for inter-cluster communications.

E. Overview of the Machine Learning Approaches used for Data Analysis

In this paper, we focus on a particular class of supervised learning methods that can be formally characterized using the statistical learning theory framework [35]. Statistical learning approaches aim to infer the function that maps input data to output data, such that the learned function can be used to predict the output from future input. In order to guarantee that the learned model generalizes well to unseen data, statistical learning algorithms try to limit the complexity of the resulting model to prevent overfitting. In particular, we use an efficient class of learning algorithms called SVM [12]. An SVM tries to achieve the best separation between patterns belonging to different classes by finding the maximum-separation hyperplane that has the largest distance to the nearest training data point of any class. In general, the larger the distance margin, the lower the generalization error of the classifier and the risk of overfitting the data. As a result, this learning framework is particularly indicated when the available data is limited. A similar framework can be applied in the case of real-valued outputs (regression tasks) using a variant called Support Vector Regression (SVR) [36]. While our database is quite broad in terms of surveyed area, it is limited in terms of number of measurements. For this reason, we have chosen SVM and SVR for the tasks of classification and regression, respectively.

We consider both linear and non-linear SVMs. In linear SVM, we assume that the patterns

are linearly separable, and find two parallel hyperplanes whose distance is as large as possible to separate the two classes of data. The equation of a linear SVM is expressed in the form

$$f(x) = \langle \vec{w}, \vec{x} \rangle + b, \quad (6)$$

where $\langle \cdot, \cdot \rangle$ denotes the inner product in \mathbb{R}^n , and the vector w and scalar b are used to define the position of the maximum-margin separating hyperplane. Geometrically, the distance between the two external hyperplanes is $2/\|\vec{w}\|$, so in order to maximize their distance we want to minimize $\|\vec{w}\|$. As we also have to prevent data points from falling into the margin, we add the following constraints $\forall i$:

$$\begin{cases} \vec{w} \cdot \vec{x}_i - b \geq 1 & \text{if } y_i = 1 \\ \vec{w} \cdot \vec{x}_i - b \leq -1, & \text{if } y_i = -1 \end{cases}. \quad (7)$$

These constraints state that each data point must lie on the correct side of the margin. By introducing Lagrange multipliers α_i , the SVM training procedure amounts to solving a convex quadratic problem. The solution is a unique globally optimum result, for which

$$\vec{w} = \sum_{i=1}^N \alpha_i y_i \vec{x}_i \quad (8)$$

The terms \vec{x}_i are called *support vectors*. Once an SVM has been trained, the decision function can simply be written as

$$f(\vec{x}) = \text{sign} \left(\sum_{i=1}^N \alpha_i y_i (\langle \vec{x}, \vec{x}_i \rangle) + b \right). \quad (9)$$

The non-linear SVM uses the so-called *kernel trick*, implicitly mapping the inputs into higher-dimensional feature spaces. The resulting algorithm is formally similar to the linear SVM, except that every dot product is replaced by a non-linear kernel function $K(\vec{x}, \vec{x}_i)$. This allows the algorithm to fit the maximum-margin hyperplane in a transformed feature space. In this work we use the popular Gaussian Radial Basis Function (RBF) kernel:

$$K(\vec{x}, \vec{x}_i) = \exp \left(- |\vec{x} - \vec{x}_i|^2 / (2\sigma^2) \right). \quad (10)$$

III. DESCRIPTION OF THE ACQUIRED DATASET

To validate our system we used a data set collected during the NATO ALOMEX 2015 mission. The ALOMEX 2015 experiment spanned 13 days across 2800 km from southern Spain to west Africa. During this expedition, we measured both acoustic and optical link properties in the nine different stations marked in Fig. 1. Some stations were sampled in the same locations but at different times. In each station, a data collection lasting over an hour took place.

The locations noted in Fig. 1 were chosen to represent different channel conditions, as reported in Table I. Note that Stations 1-4

were located in the Mediterranean Sea, while Stations 5-9 were sampled in the Atlantic Ocean.

The measurement equipment was hosted on board the 93 m-long R/V Alliance. The optical properties were evaluated by probing the water column from the bow of the Alliance, while the transmissions took place from the stern. In two locations, the acoustic transmissions were performed from a work boat located approximately 1000 m from the Alliance. Referring to Fig. 1, these locations were Station 3, in the Alboran Sea ($35^{\circ}47.0453' N$, $004^{\circ}51.0284' W$), and Station 4, in the Atlantic Ocean along the Moroccan coast ($30^{\circ}42.5113' N$, $010^{\circ}18.6613' W$). Acoustic measurements were obtained by transmitting and receiving acoustic signals covering two different frequency bands. In all cases, the receiver and transmitter were deployed horizontally.

The dataset employed in this study is available online at <http://marsci.haifa.ac.il/share/diamant/DataToShare.zip> in the form of two 3-D matrices for the acoustic and optical data. Each matrix contains the time-varying measured acoustic and optical properties for each experiment station. Below, we describe the measured acoustic and optical properties in more detail.



Fig. 1. Location of the measurement sites during the ALOMEX'15 cruise. Some stations were sampled at the same location but at different times.

TABLE I
EXPERIMENTAL MEASUREMENT STATIONS

#	Location	Date	Time	Temp.	Depth	Range	Notes
1	37°35.3729'N, 00°58.7448'W	Nov 1	13:40	18°C	20 m	21 m	Cartagena Harbor, instruments calibration
2	36°25.0708'N, 01°40.0358'W	Nov 2	14:00	21°C	128 m	52 m	Rough sea, average wave height of 1 m
3	35°45.4758'N, 04°55.6935'W	Nov 4	12:30	19°C	129 m	57 m	Calm sea
4	35°47.0453'N, 04°51.0284'W	Nov 4	16:30	20.5°C	119 m	1.3 km	Calm sea, working boat
5	30°42.5113'N, 10°18.6613'W	Nov 6	09:00	20.5°C	127 m	1 km, 583 m	Calm ocean, working boat
6	30°28.5720'N, 10°16.5030'W	Nov 6	15:30	20.5°C	126 m	59 m	Calm ocean
7	23°51.1912'N, 16°19.4189'W	Nov 9	15:30	19.5°C	40 m	45 m	Shallow/warm/turbid waters (Sahara sandstorm)
8	25°04.0009'N, 15°20.4917'W	Nov 10	09:30	22°C	44 m	51 m	Calm ocean with clear waters
9	25°13.1351'N, 15°30.1324'W	Nov 10	13:45	22°C	77 m	53 m	Calm ocean with clear waters

A. Acoustic Properties

In the absence of a theory connecting underwater acoustics and underwater optics, to statistically explore the relation between AC and OC we utilize all acoustic properties we could measure. The analysis below will show that no specific acoustic property is individually dominant to characterize the quality of an optical link. The acoustic dataset includes a total of 9 and 6 properties for the LF and HF bands, respectively, due to the different parameter set that the LF and HF devices could measure. A summary of the properties is provided for reference in Table II.

The acoustic measurements were collected in a lower frequency (LF) band of 8-16 kHz, and in a higher frequency (HF) band of 18-34 kHz. LF involved the transmission of 200 consecutive linear frequency modulated (LFM) signals of duration 0.1 s and with a guard interval of 0.1 s. The LFM LF signals were transmitted through an omni-directional ITC projector at a source level of 181 dB Re 1 μ Pa @ 1 m (with a ripple of 3 dB in the frequency range considered), and received

TABLE II
ACOUSTIC PROPERTIES MEASURED DURING THE TRIAL.

#	Parameter	Measurement
Lower frequency range		
1	Noise level (LF)	Average value of $\rho_{MF}(\tau)$ before the arrival of the first path
2	RSSI (LF)	Value of the first valid peak in $\rho_{MF}(\tau)$
3	Delay spread (LF)	RMS of delay of valid peaks in $\rho_{MF}(\tau)$
4	RMS tap amplitude (LF)	RMS of valid peaks in ρ_{MF}^i
5	Number of paths (LF)	Number of valid peaks in $\rho_{MF}(\tau)$
6	SNR (LF)	Ratio between the received energy and the noise level
7	Channel length (LF)	Difference between the arrival delays of the last and first valid peaks in $\rho_{MF}(\tau)$
8	Noise coherence (LF)	Average time for which the cross-correlation between noise level measurements decreases below 90%
9	Coherence time (LF)	Average time $x T_s$ for which the cross-correlation between $\rho_{MF}(\tau)$ and $\rho_{MF}(\tau + \Delta)$, for some Δ , decreases below 90%
Higher frequency range		
1	Noise (HF)	Measured noise level
2	RSSI (HF)	Indicator for the received signal strength
3	Delay spread (HF)	RMS of delay of measured channel taps
4	RMS tap amplitude (HF)	RMS of measured channel taps
5	Number taps (HF)	Number of measured channel taps
6	Integrity (HF)	Indicator for link quality

by two omni-directional Cetacean C57 hydrophones with flat receiver sensitivity, one placed at a depth of 5 m and a second one placed at a depth of 10 m. The pre-amplification level of these two hydrophones was 20 dB. In parallel to the transmissions in the LF band, the acoustic properties in the HF band were measured by a pair of EvoLogics S2C acoustic modems in the range 18-34 kHz, transmitting omni-directionally with a source level of 184 dB re 1 μ Pa @ 1 m (with a ripple of about 5 dB in the frequency range considered), both deployed at a depth of 10 m. The modems set their pre-amplification level automatically based on the level of the first received signal, and reception was also omni-directional with a flat receiver sensitivity.

Lower Frequency (LF) Band — The LFM signals recorded by the hydrophone were cross-correlated to estimate the channel impulse response and to evaluate the noise characteristics. To that end, we used a matched filter (MF). Let $s(t)$ $0 < t \leq T_s$ be a transmitted LFM signal of unit

energy and duration T_s s, and let $y(t)$, $0 < t \leq T_s + T_d$ be the corresponding signal at the output of the channel, with T_d being the delay spread of the channel. The non-normalized MF output is given by

$$\rho_{\text{MF}}(\tau) = \left| \int_0^{T_s} s(t)y(t - \tau) dt \right|. \quad (11)$$

Since $s(t)$ is a wideband LFM and since the SNR is high, ρ_{MF} is an approximation of the channel impulse response $h(\tau)$ [37]. This is because, assuming that the channel impulse response $h(\tau)$ is linear, the following simplification may be made:

$$\int_0^{T_s} s(t)y(t - \tau)dt = \int_0^{T_s} s(t) (s(t) * h(t - \tau)) dt \approx \int_0^{T_s} \delta(t)h(t - \tau)dt = h(\tau), \quad (12)$$

where $\delta(t)$ is the Dirac delta function, and $*$ denotes convolution.

To evaluate which of the peaks in ρ_{MF} corresponds to true arrivals, we used a constant false alarm threshold. Since setting a threshold directly on the response ρ_{MF} requires the evaluation of the noise power spectral density (psd), which can be time-varying and hard to track, we used the normalized MF whose response is

$$\rho_{\text{NMF}} = \frac{|\int s(t)y(t) dt|}{\sqrt{\int s^2(t) dt \int y^2(t) dt}}. \quad (13)$$

As we recently showed in [38], given a target false alarm probability, P_{fa} , a threshold x_T can be set without the need to estimate the noise characteristics. This threshold is calculated by

$$P_{\text{fa}} = 1 - B\left(x_T^2, \frac{1}{2}, \frac{N-1}{2}\right), \quad (14)$$

where N is the product of the signal bandwidth and duration T_s , and

$$B(a, b, z) = \int_0^a t^{b-1}(1-t)^{z-1} dt$$

denotes the regularized incomplete beta function [39]. As the locations of the valid peaks in ρ_{NMF}^i correspond to those in ρ_{MF}^i , these peaks are used to determine the acoustic properties. As the acoustic properties affecting OC are unknown, we have chosen to employ all main acoustic link properties which could be extracted from the received LFM signals. This list is described in Table II.

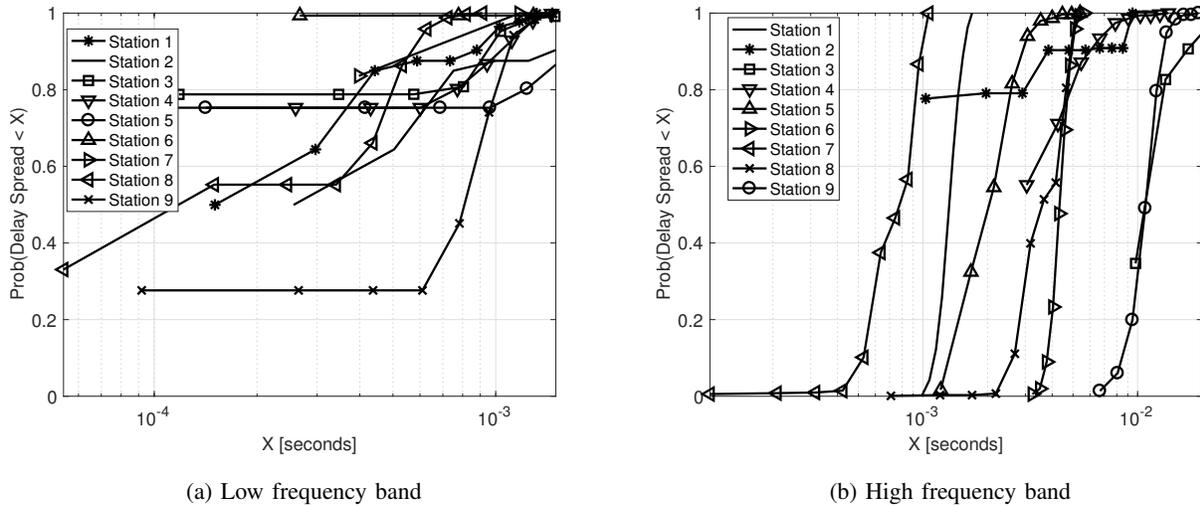


Fig. 2. CDF of the delay spread in the LF and HF bands for the measurement stations (note the different x-axis scale).

Higher Frequency (HF) Band — The acoustic properties in the HF band were calculated by the firmware of the EvoLogics modem. For each communication packet, the modems provide an estimate of the received signal strength indicator (RSSI), the power and delay of the most significant multipath arrivals, the noise level, the propagation delay, and an empirical evaluation of the communication link’s integrity. The latter measurement reflects the SNR, hence the bit error rate. The acoustic properties given by the EvoLogics modems in the HF band are the received energy, the noise level, the SNR, the number of paths, the delay spread, and the integrity.

In Figs. 2a and 2b, we show the per-site cumulative distribution function (CDF) of the delay spread parameter in the LF and HF bands, respectively. The results highlight significant differences across the sites. For example, we observe an order of magnitude difference between the delay spread of the HF at site 6 compared to site 9, and the variance of the delay spread of the LF at site 8 is much bigger than that at site 4. This corroborates the requirement to perform measurements in different environments. This inter-site variability guarantees that the learning algorithms extract robust statistical correlations among the signals, which can be validated on separate, different subsets of patterns used during the test phase.

While the number of measurements and the number of parameters available at HF are relatively

small, the SVM and the SVR can learn robust models even with a very small number of training samples [40], [41]. In our case, this is also supported by the fact that the measurements at HF are distributed fairly equally across all the sites, thereby representing a heterogeneous distribution.

B. Optical Properties

The optical parameters of the water were measured using a Wet Labs Conductivity, Temperature and Depth (CTD) system with an AC-s meter [9], and the free-falling Satlantic Hyperpro II radiometer [8]. The CTD provided measurements of the optical absorption and attenuation coefficients, water salinity, conductivity, temperature and sound speed throughout the water column. The optical profiler measured the downwelling radiance along the so-called euphotic zone while the boat was moving straight at a constant speed. The data was collected at several wavelengths from 400 nm to 735 nm.

Using these devices, we obtained a set of physical characteristics for different depth and wavelength including the absorption rate, a , the attenuation rate, c , and the water temperature, T . Using a and c , the scattering rate b is calculated via (2). Parameters c and T were processed to evaluate the SNR of the underwater optical link at different depths, wavelengths, and distances from the source. In particular, following the model in [2] and assuming a perfect alignment between the transmitter and the receiver, the optical SNR at range r and depth d is computed as

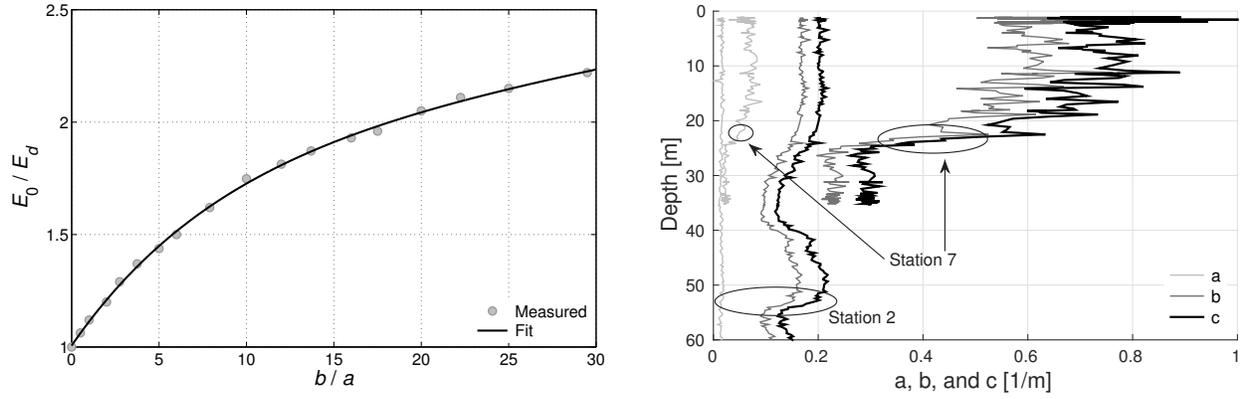
$$SNR_o(r, d) = \frac{P_0 S \frac{2A_r}{\pi r^2 (1 - \cos \theta) + 2A_t} \exp(-c(d) \cdot r)}{(E_0(d) A_r S)^2 + 2q(I_d + I_\ell)B + 4KTB/R}, \quad (15)$$

where the notation and the values assigned to each parameter are summarized in Table III.

At each measurement site, the optical SNR was evaluated for four ranges and four depth values, namely $r \in \{5, 10, 15, 20\}$ m and $d \in \{5, 10, 20, 35\}$ m, and at a single wavelength of 532 nm.

In (15), the parameter E_0 has been chosen to represent two cases:

- 1) *Dark waters*: optical transmission during the night. Here we set $E_0 = 10^{-6}$ W/m² as a realistically low value that represents a negligible light background.
- 2) *Daytime*: optical transmission in the presence of solar light noise. Here, E_0 is computed based on the output of the HyperPro profiler.



(a) Relationship between E_0/E_d and b/a , used to measure E_0 in the presence of solar light. (b) Measured absorption (a , light gray) scattering (b , dark gray) and total attenuation (c , black) coefficients for stations 2 and 7.

Fig. 3. Parameters of underwater optical communications: (a) E_0/E_d vs. b/a ; (b) sample plots of a , b and c at two stations.

Since the HyperPro measures only the downwelling radiance per unit wavelength E_d in $W/(cm^2 nm)$, in the second case we applied a conversion based on the relation between ratio E_0/E_d and ratio b/a [42, page 180]. This relationship is illustrated in Fig. 3a. Our dataset includes one set of optical parameters measured at each site per depth and wavelength. From this data, we evaluate one SNR value per pair of depth and transmission distance.

Two example measurements of the parameters a , b and c obtained at Stations 2 and 7 of the ALOMEX 2015 campaign are shown in Fig. 3b. The variation of a with depth is depicted via a light gray line, the variation of b via a dark gray line, and the variation of c via a black line. The mixed waters of Station 2 are reflected by some irregularities in the variation of b with depth. The turbid waters of Station 7 display a higher scattering coefficient b at all depths, characterized by

TABLE III

OPTICAL PROPERTIES: NOTATION AND MEANING

Meaning	Value	
P_0	Source-radiated optical power	30 W
S	Receiver sensitivity	0.26 A/W
A_r	Receiver area	1.1 mm ²
A_t	Transmitter's area	10 mm ²
θ	Transmitter's semi-aperture	0.5 rad
E_0	Scalar irradiance of the solar light	From measurements
q	Elementary charge	$1.6 \cdot 10^{-19}$ C
I_d	Photodetector's dark current	1 nA
I_ℓ	Incident light current	1 μ A (upper bound)
B	Signal bandwidth	100 kHz
K	Boltzmann constant	$1.38 \cdot 10^{-23}$ JK ⁻¹
T	Temperature	From measurements
R	Receiver's shunt resistance	1.43 G Ω
a	Absorption rate	From measurements
b	Scattering rate	From measurements
c	Total attenuation rate	From measurements

spikes at some depths. With reference to Table I, we observe that the mixed waters of Station 2 confer a mildly irregular variation with depth to b . On the contrary, the highly turbid waters of Station 7 are characterized by higher values of b and more irregular variations with depth. In both cases, b is the dominating parameter concurring to $c = a + b$.

IV. RESULTS FOR EVALUATING THE RELATIONSHIP BETWEEN AC AND OC

In this section, we discuss *i*) the results of the learning methods used to find the set of acoustic properties that can predict the reliability of the optical link, and *ii*) the pairs of acoustic and optical properties that show a trend of high correlation. Since the optical data included only one set of measured parameters per site, we have only performed classification and prediction from the acoustic properties to the optical properties.

In the results presented below, performance figures are shown for both a linear SVM (Lin) and a non-linear kernel (RBF). Input for classification and prediction are the LF acoustic measurements at 5 m depth (LF5), the LF acoustic measurements at 10 m depth (LF10), and the HF acoustic measurements (HF). To assess the robustness of the proposed learning system, we repeated the analysis several times, shuffling the training and test patterns before each run. Error bars in the figures indicate standard deviations computed for 10 different repetitions of this process.

A. System Model

In this work, all data processing was performed offline, including both training and testing procedures. However, the database formed by the measured AC and OC properties can also be processed online later. In this case, training is performed offline before system deployment while testing (i.e., classification) takes place online. For online applications, it is important to use a testing database containing a very diverse set of measurements. Otherwise, overfitting may occur in the training phase and online classification may fail. Since the experiment involved data collection from multiple sea and ocean environments and during both daytime and nighttime, we believe that our database achieves such diversity.

It should be noted that the performance of real OC systems depends not only on the channel parameters but also on the characteristics and deployment of optical modems. Naturally, these characteristics cannot be predicted from the AC properties. However, online prediction of the channel-based optical link quality and SNR does provide a method to evaluate OC link variation over range and depth. As mentioned in Section I, such a prediction tool can facilitate reliable communication by informing the transmitter's selection of depth and range to the receiver.

To calculate the optical SNR we make use of (15). As noted in Table III, (15) depends on some fixed properties and some measured properties. The latter include the attenuation coefficient c , the temperature T , and the light noise irradiance E_0 . The measured optical properties show, in most cases, a negligible relationship with longitude, latitude, time and depth (in line, e.g., with [43]), whereas in other cases the change with depth and location is more pronounced (as is the case, e.g., for parameter b). In both cases, we limit our study to environments where the difference in the optical properties across the locations where the acoustic and optical equipment were deployed is manageable by our model. Still, we expect to find differences in the prediction accuracy of the optical SNR and the classification of the optical link as a function of depth and range. The expected difference as a function of the depth is due to the fact that c , T , and E_0 are depth-related, and thus different correlation with the acoustic properties yields changes in the prediction accuracy. We also expect that the prediction accuracy decreases with range, as the impact of non-accurate prediction increases with range.²

While we argue that the measured optical properties do not change much in space and time, this is not the case for the acoustic properties. Because the acoustic channel is space and time-dependent, there may be a difference between the relation of the measured acoustic properties and the optical channel at different time instants. Yet, we assume that the basic characteristics of the acoustic channel are indeed distinctive of different sea/ocean environments. For example,

²We remark that our evaluation is limited to the sets of distances and depths considered in Section III-B. These sets could be extended to include further values, provided that a different classifier is trained for the corresponding optical data. A different approach would be to train a regression model of the optical parameters $c(d)$ and $E_0(d)$, substitute them into Eq. (15), and use the latter to predict the SNR for any r . As c can vary highly with depth (see Fig. 3b), this approach is expected to require a much larger training set, and is left as future work.

within a small area we expect the acoustic noise level to remain roughly the same, and similarly the average delay spread. We therefore aim to explore the relation between these basic (slowly changing in time and space) acoustic and optical characteristics. To that end, we do not perform prediction based on the instantaneous values of the acoustic parameters. Instead, for each test site we consider a large dataset of acoustic properties measured over tens of minutes, subdivide them into consecutive time windows, and perform prediction based on the average value of the acoustic parameters taken over each window.

To avoid prediction bias and overfitting, we performed multiple training and testing attempts. In each attempt, a random subset of the data was chosen for training and the rest for testing. Two prediction types were considered: 1) classification where using the properties of the AC we identified OC as “good” or “bad” at different ranges and depths, and 2) prediction where we used AC properties to predict the SNR of the OC link at different ranges and depths. In the following, we describe the details of these procedures.

B. Training procedure and evaluation details

For the acoustic data, the time series describing each acoustic property were first pre-processed. This included scaling individual properties to be within the interval $[0, 1]$, windowing, and averaging. Since the diversity of the measurements is important to achieve a robust classification, the window size was determined as the one that achieved the maximum average variance of the elements within each window. This window size was determined separately for each property in each frequency band and for each experiment station. For each window, the mean and variance values were given as input to the classifier. The result is a set of 18 properties for the LF band, and a set of 12 properties for the HF band. In total, the database included 1370 patterns for the LF data at 5 meters, 2320 patterns for the LF data at 10 meters, and 297 patterns for the HF data.

Since the optical data was used as labeling for training and testing only, no pre-processing was performed. In the context of multimodal systems, we focused only on classifying and predicting the optical SNR during both nighttime and daytime (see Section III-B). However, the same procedure

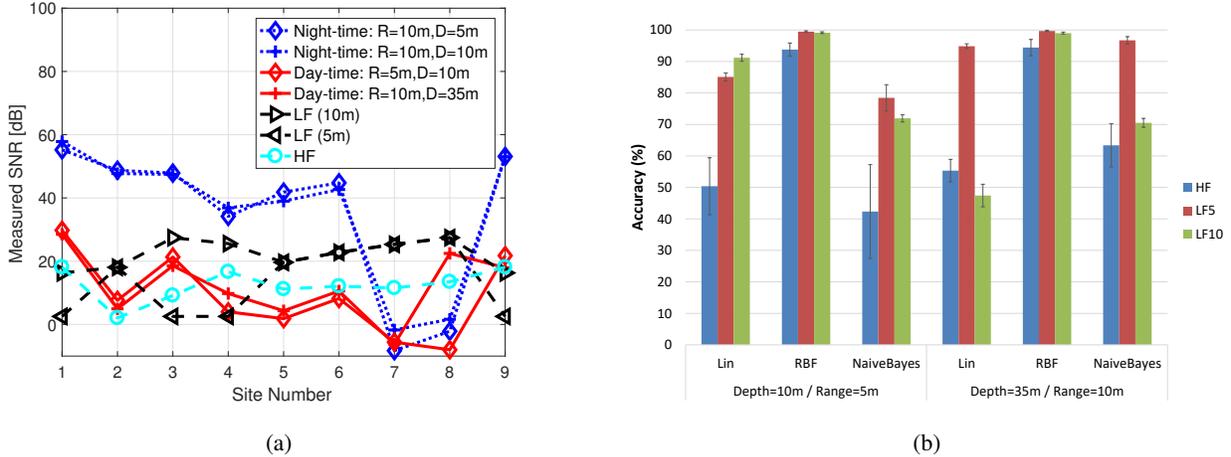


Fig. 4. (a) Average values for the optical and acoustic SNR measured at the different experimental sites. Results show a range of roughly 70 dB during nighttime, and 40 dB during daytime for optical SNR. Correlation between the optical SNR and the acoustic SNR is not clear. (b) Classification accuracy for daytime OC, obtained using linear SVM, RBF SVM, and a simple Naive Bayes classifier. Results suggest a clear non-linear relationship between acoustic properties (mostly LF5) and OC.

can be carried out for all 16 properties listed in Table III. An example for the latter is given below for parameter b .

The training procedure involved a threshold to label the trained OC dataset as “good” or “bad.” With the aim of showing the relation between AC and OC, the choice of this threshold is not necessarily related to the needs of actual OC systems, but is rather determined such that the number of “good” and “bad” training links is equalized to avoid overfitting. For the same reason, we considered only those depths and ranges that yielded a sufficient number of positive and negative OC links during the training procedure. With this in mind, for daytime measurements, we chose a fixed threshold level of 15 dB, and considered classification only for the depth-distance pairs (10, 5) m and (25, 10) m. For nighttime measurements, we chose a fixed threshold level of 10 dB, which allowed classification for all the combinations of depth $\in \{5, 10, 15, 25\}$ m and distance $\in \{10, 15, 20\}$ m. In Fig. 4a, we show the evaluated SNR of the measured OC links during daytime and nighttime. The values shown lead to a variation of roughly 70 dB in the range of SNR. Naturally, this produces a large change in the number of “good” and “bad” OC channels.

More specifically, the choice of these threshold levels yielded on average a ratio between “good” and “bad” channels of 62% for daytime and 65% for nighttime. Note that thresholding is required only for classification. For regression, instead, the whole dataset was used to train the system and predict the SNR of OC.

Training was performed separately for the acoustic LF recordings at 5 m, the acoustic LF recordings at 10 m, and the acoustic HF recordings (10 m). The aim of training was twofold: 1) discriminating the corresponding quality of the optical signal (binary-valued classification task), and 2) predicting the corresponding optical values (real-valued regression task). To that end, the dataset was first divided into training sets (75% of the patterns) and test sets (25% of the patterns), and the latter were used to test the generalization capability of the models. We considered two kernel functions: the simple linear SVMs, and the non-linear RBF kernel. To set the learning hyperparameters, we adopted a k-fold cross-validation procedure, where one fold was randomly selected and left out to test the current settings of the hyperparameters. Based on the amount of available data, we used 3 folds for LF at 5 m, 4 folds for LF at 10 meters, and 5 folds for HF. To evaluate the robustness of our approach and to reduce the risk of overfitting, each SVM was trained 10 times, and we report the mean classification accuracy and the corresponding standard deviations.

C. Classification results

The classification accuracy for the test sets is reported in Fig. 4b for both the linear SVM and the non-linear SVM with the RBF kernel. We explore classification using all three types of acoustic measurements. In all cases, the marked difference between the linear SVM and the RBF kernel suggests that the relation between the acoustic properties and the optical link quality is non-linear. In order to better assess the robustness of the findings, as a control simulation we also performed the same classification task using a Naive Bayes classifier [44]. The average accuracy obtained using this alternative type of algorithm was closely aligned with that obtained with the linear SVM (see Figure 4b). For this reason, in the following experiments we only considered the SVM models.

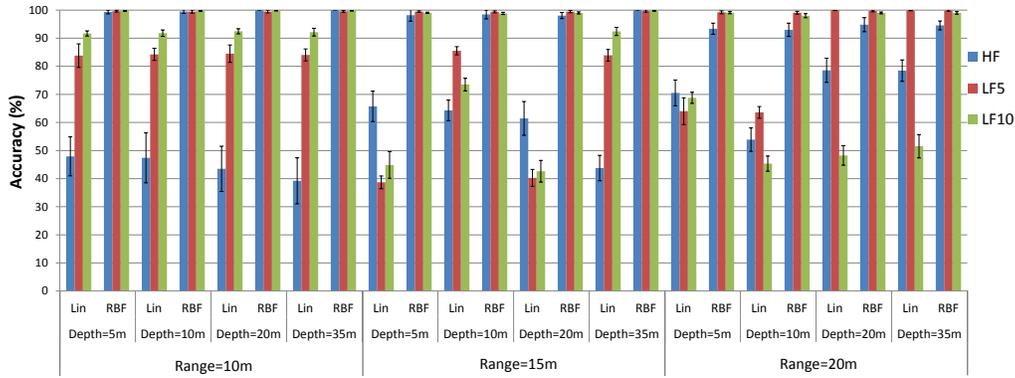


Fig. 5. Nighttime optical SNR. Results suggest a clear non-linear relation between acoustic properties and OC.

Moreover, overall the results indicate that the LF measurements provide a more accurate prediction of the quality of the optical link, approaching 100% of classification accuracy for the non-linear SVM. The LF measurements yield a much higher accuracy also for the linear SVM, except for the condition corresponding to a depth of 35 m and a range of 10 m, where the performance of LF10 is similar to that obtained using HF.

The classification accuracy for the test sets to predict the optical SNR during nighttime is reported in Fig. 5. Here, many more values of optical SNR can be predicted. Also in this case, the non-linear kernel clearly outperforms the linear SVM, achieving 100% for all the target properties. In fact, for many properties, the performance of the linear SVM in Fig. 5 is close to chance level (50%). Similar to the case of daytime optical transmission, in the nighttime scenario the LF measurements (LF5 in particular) are better predictors for the quality of the optical link. However, when using the linear SVM, HF sometimes still outperforms LF10, especially for the conditions corresponding to long distances (range = 20 m). This suggests that in nighttime conditions the HF signal can be more reliable than in daytime conditions, approaching a prediction accuracy of 100% for the non-linear SVM and of 80% for the linear SVM at long ranges.

The high classification accuracy obtained for both the daytime and the nighttime prediction of the quality of the optical link suggests a strong relationship between the acoustic properties and the OC quality. This relation seems to be non-linear, as the greatest accuracy is achieved

TABLE IV
PRECISION, RECALL AND SPECIFICITY VALUES FOR ALL THE CLASSIFICATION TASKS.

	Range (m)	Depth (m)	Linear SVM									Non-linear RBF kernel								
			HF			LF5			LF10			HF			LF5			LF10		
			Prec	Recall	Specif	Prec	Recall	Specif	Prec	Recall	Specif	Prec	Recall	Specif	Prec	Recall	Specif	Prec	Recall	Specif
Daytime	5	10	0.37	0.38	0.58	0.76	0.93	0.79	0.88	0.95	0.87	0.93	0.90	0.96	0.99	0.99	1.00	0.99	0.99	0.99
	10	35	0.53	0.40	0.70	0.57	0.97	0.95	0.27	0.44	0.49	0.96	0.92	0.96	1.00	0.96	1.00	0.98	0.99	0.99
Nighttime	10	5	0.75	0.51	0.39	0.96	0.85	0.77	1.00	0.91	0.96	0.99	0.99	0.97	1.00	1.00	0.98	1.00	1.00	0.98
		10	0.76	0.51	0.31	0.96	0.85	0.79	0.99	0.92	0.94	0.99	0.99	0.97	1.00	1.00	0.97	1.00	1.00	0.98
		20	0.82	0.46	0.21	0.96	0.85	0.81	0.99	0.92	0.92	1.00	1.00	1.00	0.99	1.00	0.97	1.00	1.00	0.99
		35	0.83	0.42	0.14	0.96	0.85	0.77	0.99	0.92	0.92	1.00	1.00	1.00	1.00	1.00	0.98	1.00	1.00	0.99
	15	5	0.81	0.74	0.32	0.37	0.21	0.59	0.52	0.45	0.45	0.98	0.98	0.95	0.99	1.00	0.99	0.99	1.00	0.98
		10	0.80	0.72	0.39	0.96	0.87	0.78	0.83	0.82	0.46	0.99	0.99	0.96	1.00	1.00	0.97	0.99	1.00	0.96
		20	0.76	0.72	0.25	0.40	0.23	0.61	0.49	0.38	0.49	0.99	0.99	0.96	0.99	1.00	0.99	0.98	1.00	0.98
		35	0.84	0.45	0.29	0.96	0.84	0.80	1.00	0.92	0.97	1.00	1.00	1.00	1.00	1.00	0.99	1.00	1.00	0.98
	20	5	0.79	0.80	0.48	0.58	0.86	0.45	0.64	0.92	0.44	0.96	0.96	0.89	0.99	1.00	0.99	0.98	1.00	0.98
		10	0.51	0.67	0.42	0.57	0.87	0.43	0.21	0.36	0.49	0.95	0.95	0.95	0.99	1.00	0.99	0.99	0.94	0.99
		20	0.84	0.85	0.65	0.99	1.00	1.00	0.24	0.39	0.52	0.99	0.99	0.98	0.94	1.00	1.00	0.96	1.00	0.99
		35	0.84	0.87	0.59	0.98	0.99	1.00	0.25	0.40	0.56	0.99	0.99	0.98	0.97	1.00	1.00	0.96	1.00	0.99

by the SVM using the RBF kernel. In order to better evaluate the classifier performance across different conditions, three additional performance measures were also computed from confusion matrices [45]: precision (i.e., class agreement of the data labels with the positive labels given by the classifier), recall (i.e., effectiveness of the classifier to identify positive labels), and specificity (i.e., effectiveness of the classifier to identify negative labels). The complete results are reported in Table IV. Precision, recall and specificity values are consistent across conditions, and fully aligned with the accuracy results reported in Fig. 4b and Fig. 5. In particular, results show that indeed the non-linear classifier achieves much better performance on all metrics, and has no biases for any particular class.

Interestingly, the data seem to suggest that linear classification using LF measurements improves close to the surface. This needs to be investigated further, as not all collected data shows this same trend, and we have no further evidence to prove it. However, we still conjecture that linear classification might be in fact more precise near the surface. A possible explanation can be a high concentration of biological particles such as plankton in the upper water layer, which would

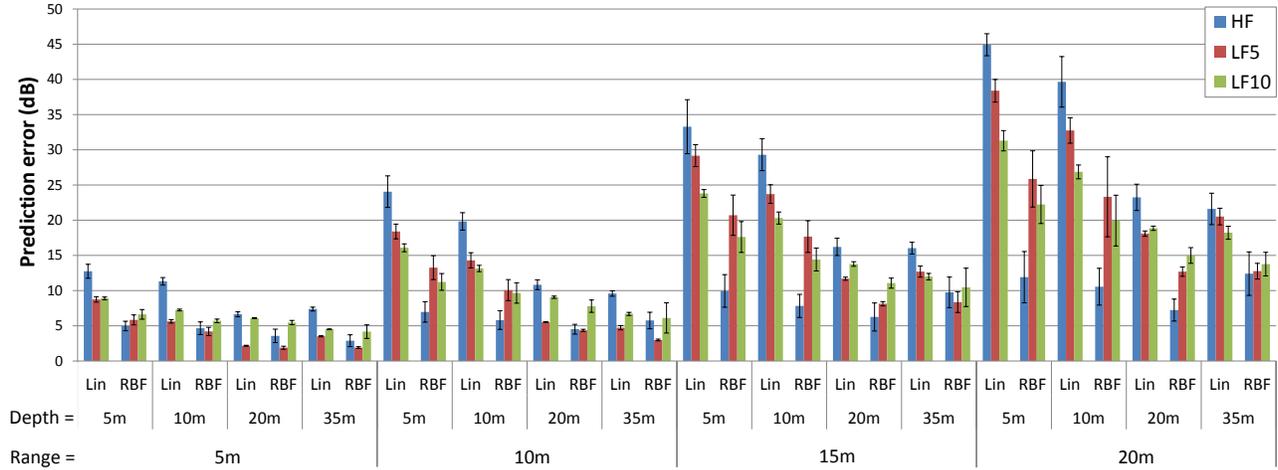


Fig. 6. Prediction error for the daytime optical SNR. Compared to the range of optical SNR, results suggest a good non-linear prediction of the optical link quality from the acoustic properties.

scatter the acoustic wave and, during daytime, also sunlight. The collection of additional data in this specific scenario would be a necessary step to verify this conjecture.

D. Prediction results

Classification results show evidence of a relationship between acoustic properties and optical link quality. The strength of this relationship can be evaluated by prediction. The optical SNR prediction errors for the test sets for all the 16 range-depth pairs of the daytime optical data are reported in Fig. 6. Refer to Fig. 4a for the true optical SNR values at the different sites and for daytime and nighttime data collection. The results are given in terms of the root mean squared error (RMSE), measured in dB, for each type of AC dataset. As observed in the classification results, the non-linear kernel outperforms the linear SVM when predicting SNR. Notably, the RMSE of optical SNR achieved by the non-linear SVM is always around or below 5 dB at any measured depth when the range is 5 m. Contrary to the classification task, using HF acoustic data to train the RBF SVM for regression yields, in most cases, results that are better than those achieved using LF acoustic data. This result might be due to the fact that the binary classification task is easier to perform than the fine-grained regression task, which could be more challenging to fulfill at high

accuracy. The larger number of samples in the LF dataset might have introduced noise that was detrimental only for the fine-grained predictions performed with the non-linear SVM.³

The optical SNR measured at several depths and ranges as well as the average measured acoustic SNR values are shown in Fig. 4a. No clear correlation is visible at this point between the optical and acoustic SNR values for the different testing sites. The optical SNR varies between -10 dB and 60 dB for nighttime OC, and between -10 dB and 30 dB for daytime OC. Within such broad ranges, being able to predict the optical SNR based on acoustic SNR measurements within roughly 5 dB of RMS error strongly suggests the existence of a relationship between AC and OC. We also observe that the accuracy of the prediction decreases with increasing range, and is lowest for the longest range of 20 m. Such a range is akin to the maximum operational range of several practical underwater optical modems. Therefore, the accuracy decrease is expected, and mainly due to the SNR decrease as a result of absorption and scattering of light power in water.

For the nighttime scenario, the prediction errors of the test sets for all the 16 range-depth pairs are reported in Fig. 7. Similar to the case of daytime optical transmission, we observe that the non-linear kernel operates far better than the linear one. When using RBF, the regression results obtained using the HF dataset are better than those obtained using LF5 and LF10, which might be due to overfitting. Although this trend was observed also in daytime conditions, this difference is much more marked in nighttime conditions.

We now consider optical-SNR prediction accuracy as a function of depth. By analyzing the trends in Fig. 7, we observe that for the RBF kernel, the prediction error at a fixed distance (i.e., for each different range) gradually decreases with depth. Hence, the optical signal becomes more predictable as we move deeper in the water. However, this interesting trend holds only for the first three depths, while at a depth of 35 m we notice that the prediction error remains about the

³Another possible explanation is that the HF regression training was overfitting the results. We have found a marked difference between an accuracy of 0.5 dB in training and 2 dB in testing that may support this, where on the contrary, the LF error was comparable between training and test sets. However, since the test performance of the non-linear SVM using HF was often lower than that obtained with LF, this explanation is not supported by sufficient evidence.

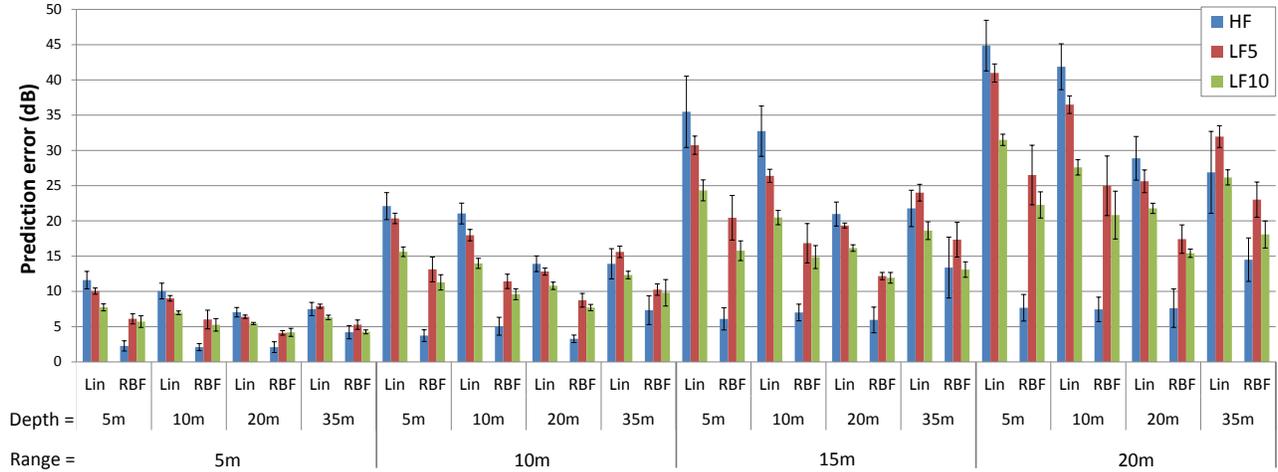


Fig. 7. Prediction error for nighttime optical SNR. Compared to the range of optical SNR, results suggest a good non-linear prediction of the optical link quality from the acoustic properties.

same or slightly increases. This phenomenon occurs for prediction using both LF and HF acoustic measurements, and means that, up to a certain depth, the optical SNR becomes more predictable. We argue that this effect is due to the scattering coefficient b which decreases with depth up to a certain value, as seen in Fig. 3b. As long as b decreases, the exponential parameter in (15) becomes less dominant, and predicting the optical SNR becomes easier. Note that this effect appears even if the actual value of b cannot be predicted accurately per se. In order to test this hypothesis, we trained the RBF SVM to predict the observed parameter b . The results shown in Fig. 8 imply that it is harder to predict the value of b at a depth of 35 m. The reason behind this is that scattering tends to happen mostly in the euphotic zone of the water column, whose boundaries are limited to specific water depths. When optical measurements are performed deeper than the euphotic zone, b tends to drop, as observed, e.g., from Station 7 data in Fig. 3b. Such a drop may not be captured by the training over the rest of the data set, which explains the RMSE increase in Fig. 8 at a depth of 35 m. Remarkably, this does not greatly affect the accuracy of the SNR prediction, because a lower b also means that the SNR would be less affected by the exponential parameter in (15).

E. Impact of single properties on prediction accuracy

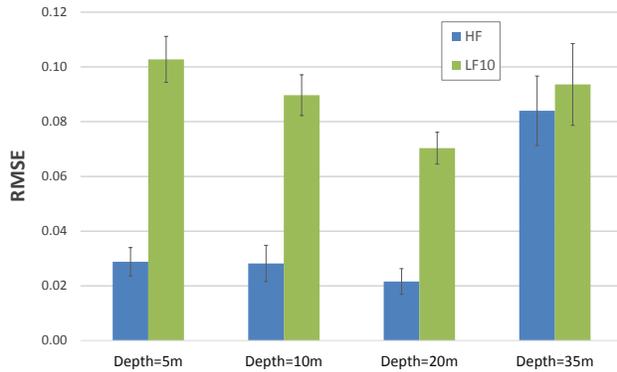


Fig. 8. RMSE for the prediction of the scattering parameter b using the RBF SVM kernel.

We now wish to explore if there are certain acoustic properties which are more closely related to the optical properties and are thus more informative for optical channel quality prediction. We therefore investigate the influence of each individual acoustic property on the prediction accuracy of the optical SNR. To that end, in this section,

instead of performing prediction based on the full set of nine (LF) and six (HF) acoustic properties, we perform prediction based on each of the measured properties independently.

In Fig. 9, we show the daytime and nighttime prediction error of the optical SNR, respectively, evaluated for a transmission range of 5 m, and averaged across the four considered depth values. The enumerated properties match those in Table II. As expected, the average prediction accuracy decreases when using only a single acoustic property as the predictor. For the nighttime case, this result is observed when using both the lower and the higher frequency acoustic properties. However, for regression of the optical SNR during daytime, this performance decrease is mostly observed when using the HF data, and the decrease when using the LF data is only marginal. Compared with the prediction performance when using all properties (column “All param” in Fig. 9), we note that the prediction error increases only by roughly 3 dB. This result suggests that even when not all considered acoustic properties are available, the relationship between AC and OC is sufficiently marked to allow the prediction of the optical SNR. (Recall the intuitive explanation for this result given in Section II-C.)

From Fig. 9, we observe that the average error is fairly constant across all single acoustic properties. This suggests that the acoustic properties used have a similar correlation with the optical properties. That is, no specific acoustic parameter is dominant for predicting the SNR of the optical link. Yet, exploiting the whole set of parameters yields better performance, as the prediction error decreases from 5–8 dB to 3–5 dB. In particular, the first set of bars in each panel

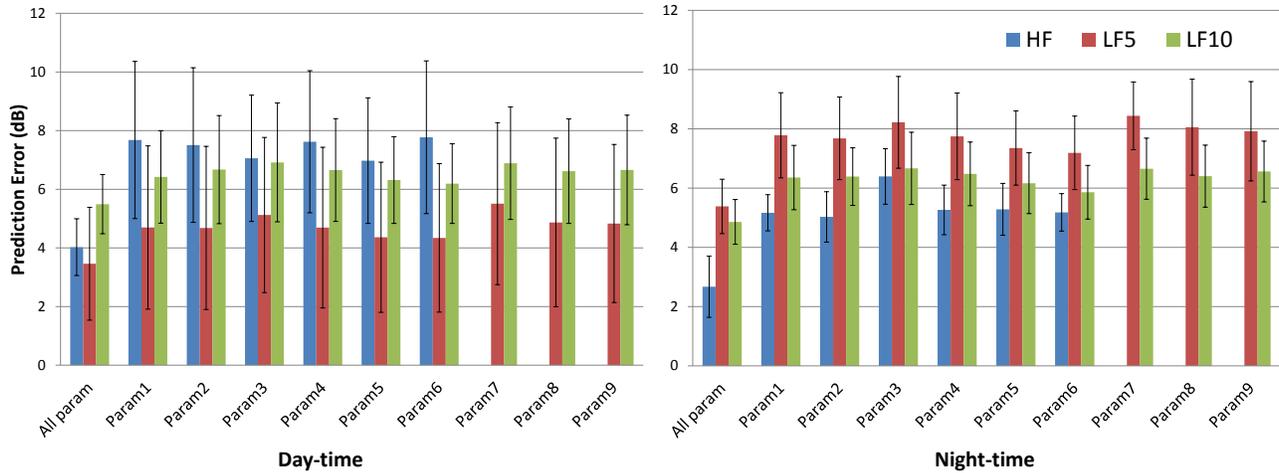


Fig. 9. Prediction error of the optical SNR for range 5 m averaged for all depths (5, 10, 20 and 35 m). Results obtained using the SVM with the RBF kernel, trained with either all acoustic properties or a single property at a time.

of Fig. 9 (“All param”), show that for the range of 5 m, the prediction error performance is about 5 dB. From this result, we conclude that the theoretical relation between the AC and the OC are quit complex and cannot be simplified based on a single AC parameter.

From Figs. 6 and 7, we observe that the prediction performance improves as the range decreases. As is even clearer from the average results shown in the first column of Fig. 9 (“All param”), we also observe that the prediction results for the nighttime optical SNR are generally better than for the daytime SNR at 5 meter ranges. Performing this same analysis for ranges of 10 m, 15 m, and 20 m also revealed generally better optical-SNR prediction results at night. Both trends are explained due to a more complex connection between AC and OC as range and sunlight increase. Both make predictions more demanding as an accurate evaluation of the parameters c and E_0 is respectively required in these cases (see Table III).

F. Implications for multimodal technology switch mechanisms

Given the range of the optical SNR as shown in Fig. 4a, the results for both nighttime and daytime classification and regression show a fairly accurate prediction of the optical SNR. This performance not only strengthens the evidence of a connection between the acoustic properties

and the optical ones, but also implies that the practical application of directing an autonomous underwater vehicle (AUV) to the optimum range and depth for OC is realistic. That is, the AUV can head directly to a location predicted to have good optical SNR, while still being deep enough and far enough from the vessel it communicates with for safety reasons. In this context, the mission of the AUV will be to communicate optically when in range, by keeping a safe distance to the communicating vessel.

For a target optical SNR, T_h , the following algorithm can be applied:

- 1) Train an acoustic-optical classifier and predictor based on collected data (the database openly shared with this paper);
- 2) Collect acoustic properties to form an input data set;
- 3) Given range and depth, classify the quality of OC and predict the optical SNR, $\text{SNR}_o(r, d)$;
- 4) Direct the AUV to a location at range \hat{r} and depth \hat{d} for which OC is classified as a good link, and for which $\text{SNR}_o(\hat{r}, \hat{d}) > T_h$, and switch from AC to OC.

V. CONCLUSIONS

In this work, we explored the statistical relationship between the properties of underwater acoustic and optical links for the purpose of classifying the underwater optical link and predicting its SNR. We based our analysis on a large database including both optical and acoustic measurements, collected in nine different sea environments during a 13-day expedition. Our results indicate a clear relation between the acoustic properties and the quality of the optical link. In particular, using the RBF classifier, with the acoustic measurements we were able to predict the quality of the optical link with an accuracy close to 100%. Moreover, for the range of 5 m, we were able to predict the SNR of the optical link with an accuracy of about 5 dB within a dynamic range of 70 dB. Our results further show that in most cases, the higher frequency measurements of the acoustic channel can better predict the optical channel. Our classification and prediction algorithms can already serve as a switching mechanism for multimodal systems that combine underwater acoustic and optical communications. While our results provide strong evidence about the connection between acoustic

and optical channels in the water, we could not develop the mathematical relation between the two channels, and this requires further exploration. As an additional future research direction, we plan to include an initial unsupervised phase, which might discover useful patterns in the data and thereby better support multiple supervised tasks. As a future direction, unsupervised learning, e.g., deep belief networks [46], [47], may discover other useful patterns in the data such as meaningful clustering of the data, and that can adaptively set the classification thresholds. Successful application of these approaches to communication systems [48], [49] motivates their use in our context as well.

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